(i) Printed Pages: 3]

Roll No.

(ii) Questions :81

Sub. Code : 0 2 4 2

Exam. Code : 0 0 0 3

B.A./B.Sc. (General) 3rd Semester Examination

1127

MATHEMATICS (Differential Equations-I)

Paper : II

Time: 3 Hours]

[Max. Marks: 30

Note: Attempt five questions, selecting at least two questions from each Unit.

Unit-I

- 1. (a) Is integrating factor of Mdx + Ndy = 0 unique. Justify.
 - (b) State and Prove sufficient condition for Mdx + Ndy = 0 to be exact. 3,3
- 2. (a) Solve: $x^{2}p^{2} - 2xyp + 2y^{2} - x^{2} = 0$ (1) Turn Over

NA-54

(b) Solve:

$$\frac{2y}{x} - p = f\left(\frac{px - y}{x^2}\right)$$
3,3

- 3. (a) Find singular solution of $3p^2e^2 px + 1 = 0$.
 - (b) Find orthogonal trajectories of family of ellipses with centres at (0, 0) and two vertices at (1, 0), (-1, 0).
- 4. (a) Solve:

$$(D^4 - D^2) y = 4$$

(b) Solve:

$$(D^2 - 4D + 4)y = e^{2x} \cos^2 x$$
 3,3

Unit-II

5. (a) Solve:

$$(x^2D^2 + xD - 9)y = 0$$

given that $y = x^3$ is a solution.

(b) Solve by method of variation of parameters:

$$(D^2 - 1)y = 2(1 - e^{-2x})^{-1/2}$$
 3,3

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(2)

6. Reduce:

$$2x^2y\frac{d^2y}{dx^2} + 4y^2 = x^2\left(\frac{dy}{dx}\right)^2 + 2xy\left(\frac{dy}{dx}\right)$$

to Cachy's form and hence solve it.

6

7. (a) Solve:

$$[(1 + x)^{2}D^{2} + (1 + x) D + 1] y$$

$$= 4 \cos [\log (1 + x)]$$

(b) Solve:

$$x\frac{d^2y}{dx^2} - \frac{dy}{dx} - 4x^3y = 8x^3 \sin x^2$$

by changing the independent variable.

3,3

3,3

8. (a) Find general solution of the linear system:

$$\frac{dx}{dt} = -2x + 7y$$

$$\frac{dy}{dt} = 3x + 2y$$

(b) Solve: Dx + 4Dy = 3y and $D^2x - Dy = 2x + 2t$

where D =
$$\frac{d}{dt}$$
.

NA-54

(3)

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